

Periodic modulation-based stochastic resonance algorithm applied to quantitative analysis for weak liquid chromatography–mass spectrometry signal of granisetron in plasma

Suyun Xiang, Wei Wang, Bingren Xiang*, Haishan Deng, Shaofei Xie

Center for Instrumental Analysis, China Pharmaceutical University, (Key Laboratory of Drug Quality Control and Pharmacovigilance, Ministry of Education), Tongjiaxiang 24, Nanjing, Jiangsu 210009, PR China

Received 5 October 2006; received in revised form 9 November 2006; accepted 10 November 2006

Available online 13 December 2006

Abstract

The periodic modulation-based stochastic resonance algorithm (PSRA) was used to amplify and detect the weak liquid chromatography–mass spectrometry (LC–MS) signal of granisetron in plasma. In the algorithm, the stochastic resonance (SR) was achieved by introducing an external periodic force to the nonlinear system. The optimization of parameters was carried out in two steps to give attention to both the signal-to-noise ratio (S/N) and the peak shape of output signal. By applying PSRA with the optimized parameters, the signal-to-noise ratio of LC–MS peak was enhanced significantly and distorted peak shape that often appeared in the traditional stochastic resonance algorithm was corrected by the added periodic force. Using the signals enhanced by PSRA, this method extended the limit of detection (LOD) and limit of quantification (LOQ) of granisetron in plasma from 0.05 and 0.2 ng/mL, respectively, to 0.01 and 0.02 ng/mL, and exhibited good linearity, accuracy and precision, which ensure accurate determination of the target analyte.

© 2006 Elsevier B.V. All rights reserved.

Keywords: Stochastic resonance; Periodic modulation; Weak signal; Granisetron; LC–MS

1. Introduction

Stochastic resonance (SR) was first introduced by Benzi et al. to explain the periodicity of Earth's ice ages [1,2]. In recent decades, SR has received increasing interest since weak signals can be amplified significantly in a nonlinear system by the assistance of noise. Typical stochastic resonance phenomena have been found in many simple physical systems [3,4] and complex chemical systems [5,6]. Its application in chromatographic analysis was first found in Pan et al.'s work [7]. And in our previous studies, it was applied successfully to quantitative analysis for weak chromatographic signals of phenazopyridine [8], glyburide [9] and roxithromycin [10] in plasma.

The algorithm based on stochastic resonance (SRA) is an efficient approach to the detection of weak signal buried in noise. However, when a chromatographic peak is extremely weak, the output signal obtained by SRA is usually distorted seriously

because of the existence of noise. It was found that the distorted signal could be corrected by introducing a periodic force into the nonlinear system, and the new algorithm was named the periodic modulation-based stochastic resonance algorithm (PSRA) [11]. Previously, PSRA has been successfully employed to improve the Roman signal of CCl_4 , but its application to chromatographic analyses has never been reported.

Granisetron is a selective 5-HT₃ receptor antagonist particularly effective for the relief of nausea and vomiting induced by cancer therapy [12]. Several methods have been reported for the determination of granisetron in biological fluids [13–15]. In the present work, liquid chromatography coupled with mass spectrometry (LC–MS) was applied to the determination of granisetron in plasma and then the LC–MS signal was processed by PSRA. By applying PSRA, the LC–MS peak was amplified significantly and characterized by good shape, and those peaks buried in noise could be determined accurately. Therefore, only small volumes were needed in the determination of plasma granisetron concentration and this was beneficial for volunteers. The limit of detection (LOD) and limit of quantification (LOQ) given by LC–MS in the current work were originally 0.05 and

* Corresponding author. Tel.: +86 25 83271180; fax: +86 25 83271454.
E-mail address: cpuxiang@yahoo.com (B. Xiang).

0.2 ng/mL, respectively. With the application of PSRA, the LOD and LOQ were, respectively, improved to 0.01 and 0.02 ng/mL. This method greatly extended the lower limit of quantification without an exhaustive exploration of the extraction methodology or a more advanced detector.

2. Theory and algorithm

The nonlinear Langevin equation has been frequently employed to describe the phenomenon of SR. It has the following formula [16]:

$$\frac{dx}{dt} = -U'(x) + MI(t) + C\xi(t) \quad (1)$$

where the variable x is the output of the nonlinear system, representing the position of signal. $I(t) = S(t) + N(t)$ denotes an input signal embedded in a noisy environment with the signal $S(t)$ and the intrinsic noise $N(t)$ caused by instrument. $\xi(t)$ is external noise added to induce the occurrence of SR. M and C , adjustable parameters, are respectively set to 1 and 0 to avoid the damage of external noise to the characteristic of intrinsic noise and reduce variable factors in SRA [7].

The symmetric double-well potential $U(x)$ used in traditional SRA can be expressed as the following equation with the constants a and b characterizing the system:

$$U(x) = -\frac{a}{2}x^2 + \frac{b}{4}x^4 \quad (2)$$

The profile of the double-well potential is presented in Fig. 1(a). Between the two stable minimum points located at $x = \pm\sqrt{a/b}$, there is a potential barrier with the height given by $\Delta U = a^2/4b$. The weak analytical signal may rest in one potential well initially. As the input signal, noise and nonlinear system match well, namely the stochastic resonance condition is reached, the weak signal can surmount the energy barrier and hop from one potential well to the other with the assistance of noise. As a result, the signal will obtain an increased intensity. However, for the relative low energy, the noise is confined in the original well with the intensity suppressed by the nonlinear system. Therefore, the output signal of the system will obtain a better signal-to-noise ratio (S/N).

When the input signal is extremely weak, the energy of the noise may be too high relative to that of useful signal and it may cause the noise to hop from one potential well to another together with the signal. As a result, the output signal will be distorted. Generally, distorted peaks are not suitable for chromatographic analysis. To correct the distorted peak shape of output signal, in this work, we added a periodic modulation into the nonlinear system [11]. Thus, the potential function can be developed into the following formula by adding such a periodic modulation:

$$U(x, t) = -\frac{a}{2}x^2 + \frac{b}{4}x^4 + x\varepsilon \sin(\omega t) \quad (3)$$

In the system described by Eq. (3), the potential barrier will vary with the periodic force (Fig. 1(b)). When the values of ε and ω are satisfactory, the signal is allowed to surmount the potential barrier while the noise is not. Thus, the peak shape of output signal will be improved.

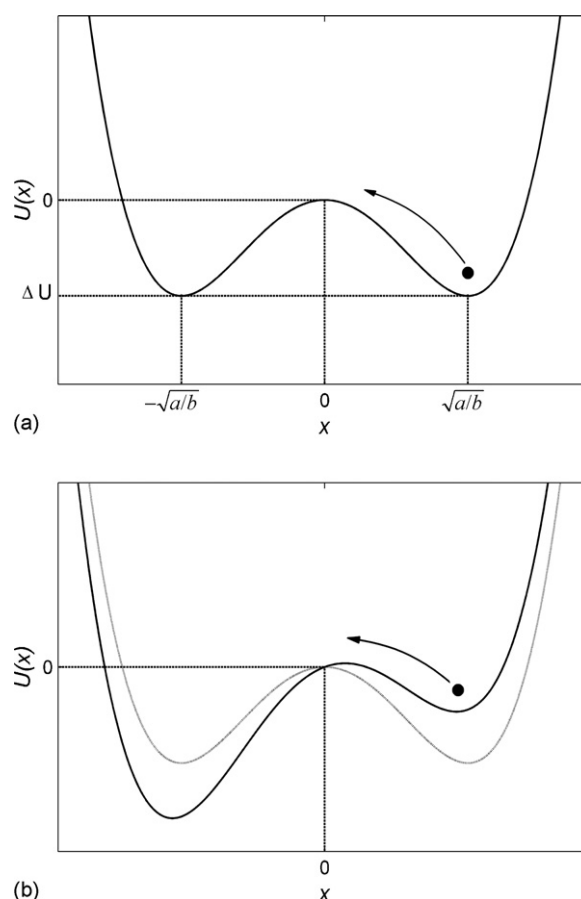


Fig. 1. The profile of double-well potential function. The potential of: (a) traditional SRA; (b) PSRA.

Eqs. (1) and (3) can be solved by a fourth-order Runge-Kutta method [17], which is more accurate than the Euler method used in the previous work [11]. Supposing that there are N sampling points in the input signal, if the n th sample of time t , the input signal $I(t)$ and the output signal $x(t)$ are denoted by t_n , I_n and x_n , respectively, the output signal can be calculated by the following equation:

$$x_{n+1} = x_n + \frac{1}{6}(k_1 + 2k_2 + 2k_3 + k_4), \quad n = 0, 1, \dots, N-1, \quad (4)$$

where k_1 , k_2 , k_3 and k_4 are given by

$$\begin{aligned} k_1 &= ax_n - bx_n^3 - \varepsilon \sin(\omega t_n) + I_n, \\ k_2 &= a \left(x_n + \frac{k_1}{2} \right) - b \left(x_n + \frac{k_1}{2} \right)^3 - \varepsilon \sin(\omega t_{n+1}) + I_{n+1}, \\ k_3 &= a \left(x_n + \frac{k_2}{2} \right) - b \left(x_n + \frac{k_2}{2} \right)^3 - \varepsilon \sin(\omega t_{n+1}) + I_{n+1}, \\ k_4 &= a(x_n + k_3) - b(x_n + k_3)^3 - \varepsilon \sin(\omega t_{n+2}) + I_{n+2}, \end{aligned} \quad (5)$$

The calculation procedure starts with the normalization of $I(t)$ to the interval $[-1, 1]$ and the normalized signal is then operated on by the algorithm to give the output signal. The final results can be obtained by inverse normalization of the output signal.

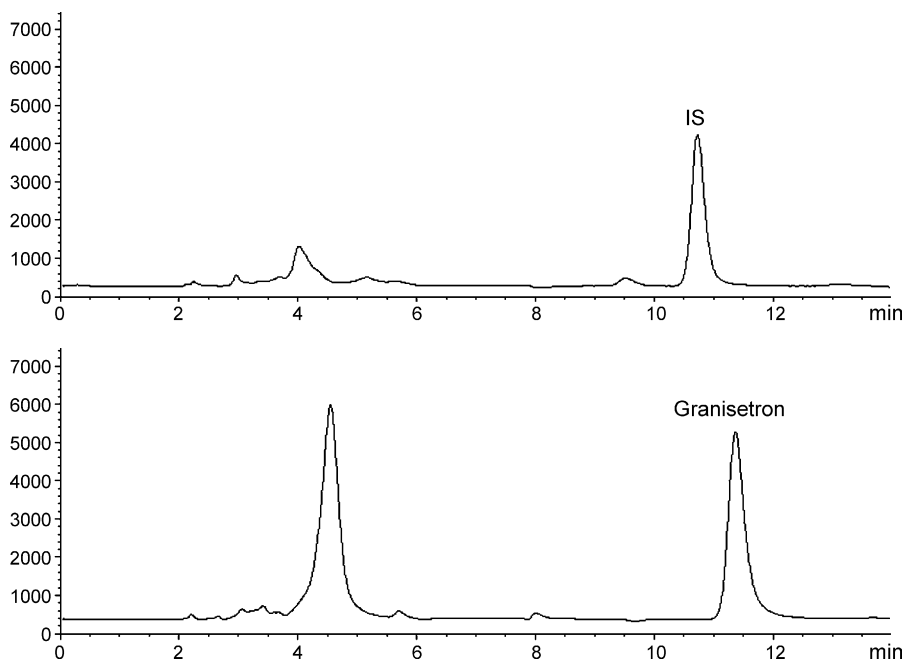


Fig. 2. Typical chromatogram of plasma spiked with IS and granisetron.

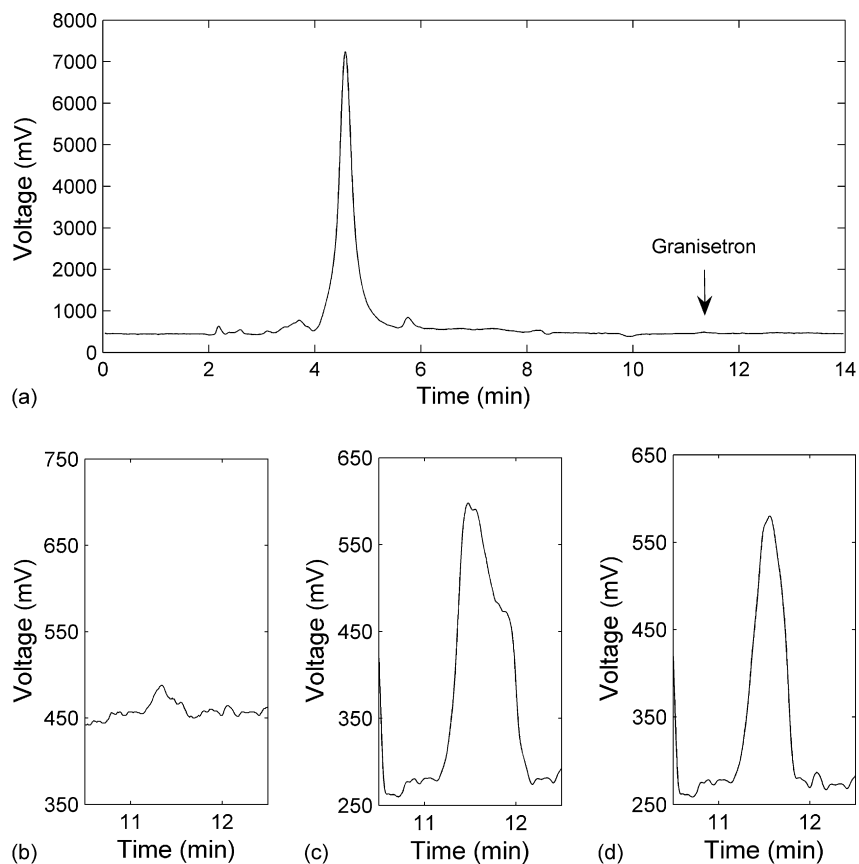


Fig. 3. Chromatogram of plasma spiked with granisetron at 0.02 ng/mL. (a) Full length of the chromatogram. (b) Especially enlarged chromatogram of granisetron. (c) The peak of granisetron obtained by traditional SRA ($a=0.17$, $b=0.0045$). (d) The peak of granisetron obtained by PSRA ($\varepsilon=0.32$, $\omega=0.31$).

[illegible]

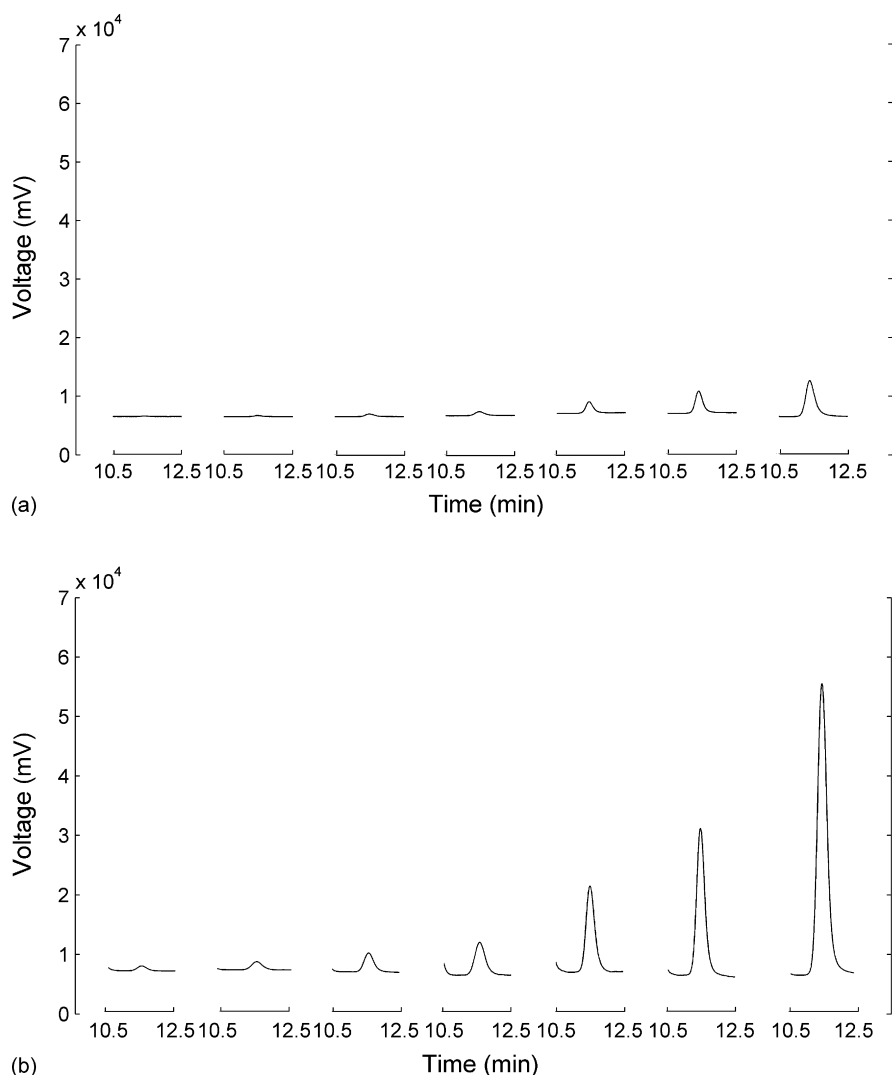


Fig. 4. Chromatograms of calibration samples of granisetron. (a) The original chromatograms of granisetron. (b) The chromatograms of granisetron obtained by PSRA ($a=0.17$, $b=0.0045$, $\varepsilon=0.32$ and $\omega=0.31$). From left to right, the concentrations of granisetron are 0.1, 0.2, 0.5, 1.0, 2.0, 5.0 and 10.0 ng/mL, respectively.

Calibration standards at seven different concentrations (0.1, 0.2, 0.5, 1.0, 2.0, 5.0 and 10.0 ng/mL) were prepared and assayed in duplicated. A good linear relationship was observed between the peak area ratio of granisetron (after PSRA) to IS (original) and the plasma concentration of granisetron (shown in Table 1). In Fig. 4, a comparison of calibration curve samples is made between the original signals and those obtained by PSRA. The result shows satisfactory amplification and good shape of the granisetron peak at each concentration when using PSRA.

The investigation of accuracy and precision was carried out with spiked preparations at concentrations of 0.2, 1.0 and 5.0 ng/mL. Intra-day accuracy and precision were determined by repeated analysis of prepared samples on one day ($n=6$), and inter-day accuracy and precision were determined by repeated analysis of prepared samples on three different days ($n=6$ series per day). The intra- and inter-day assays are summarized in Table 2 and the results indicate that the accuracy and precision of the assay are acceptable.

Table 2
Accuracy and precision of granisetron by PSRA

| Added concentration (ng/mL) | Intra-day assay | | | Inter-day assay | | |
|-----------------------------|---|--------------|-------------------------|---|--------------|-------------------------|
| | Measured concentration (mean \pm S.D.) (ng/mL) | Accuracy (%) | Precision R.S.D. (%) | Measured concentration (mean \pm S.D.) (ng/mL) | Accuracy (%) | Precision R.S.D. (%) |
| 0.2 | 0.207 \pm 0.019 | 103.5 | 9.20 | 0.204 \pm 0.024 | 102.2 | 11.90 |
| 1.0 | 0.99 \pm 0.065 | 99.4 | 6.50 | 1.01 \pm 0.071 | 100.7 | 7.02 |
| 5.0 | 4.84 \pm 0.24 | 96.8 | 4.95 | 4.92 \pm 0.29 | 99.2 | 5.89 |

5. Conclusion

To our knowledge, the application of stochastic resonance has never been reported in the LC–MS field. In the present work, the periodic modulation-based stochastic resonance algorithm was applied successfully to the detection of weak chromatographic signals from a LC–MS system. PSRA effectively corrected the distortion of peak shape that usually appeared in the traditional SRA, and provided good linearity as well as satisfactory accuracy and precision. The current work suggests that PSRA should be an effective tool in enhancing the sensitivity of mass spectrometry for the assay of therapeutic compounds and their metabolites.

References

- [1] R. Benzi, A. Sutera, A. Vulpiani, *J. Phys. A* 14 (1981) L453.
- [2] R. Benzi, G. Parisi, A. Strea, A. Vulpiani, *Tellus* 34 (1982) 10.
- [3] S. Fauve, F. Heslot, *Phys. Lett. A* 97 (1983) 5.
- [4] R. Zhu, Q.S. Li, *Phys. Lett. A* 292 (2001) 58.
- [5] W. Hohmann, D. Lebender, J. Muller, N. Schinor, F.W. Schneider, *J. Phys. Chem. A* 101 (1997) 9132.
- [6] W.M. Guo, W.S. Cai, X.G. Shao, Z.X. Pan, *Chemom. Intell. Lab. Syst.* 75 (2005) 181.
- [7] Z.X. Pan, W.M. Guo, X.J. Wu, W.S. Cai, X.G. Shao, *Chemom. Intell. Lab. Syst.* 66 (2003) 41.
- [8] Y.W. Wu, B.R. Xiang, E.X. Shang, W. Zhang, *Acta Pharm. Sin.* 40 (2005) 668.
- [9] W. Zhang, B.R. Xiang, Y.W. Wu, E.X. Shang, *Anal. Chim. Acta* 550 (2005) 77.
- [10] W. Zhang, B.R. Xiang, Y.W. Wu, E.X. Shang, *J. Chromatogr. B* 831 (2006) 307.
- [11] Z.X. Pan, X.J. Wu, W.M. Guo, W.S. Cai, X.G. Shao, *Chem. J. Chin. U* 24 (2003) 605.
- [12] H.H. Bleiberg, M. Spielmann, G. Falkson, D. Romain, *Clin. Ther.* 17 (1995) 38.
- [13] F. Pinguet, F. Bressolle, P. Martel, D. Salabert, C. Astre, *J. Chromatogr. B* 675 (1996) 99.
- [14] C. Huang, K. Chen, C. Chen, T. Tsai, *J. Chromatogr. B* 716 (1998) 251.
- [15] V.K. Boppana, C. Miller-Stein, W.H. Schaefer, *J. Chromatogr. B* 678 (1996) 227.
- [16] L. Gammaitoni, P. Hanggi, P. Jung, F. Marchesoni, *Rev. Mod. Phys.* 70 (1998) 223.
- [17] A.S. Asdi, A.H. S Tewfik, *Proceedings of the 1995 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP-95)*, Detroit, MI, 1995, p. 1332.